

p-p. Les angles que forment les liaisons hydrogène avec les directions de valence S-O des ions $S_2O_6^{2-}$, sont proches de 110° . L'hybridation des oxygènes semble donc être uniformément sp^3 .

Malgré la proximité relative, des protons appartenant à différentes molécules d'eau, les raies de résonance ne font pas apparaître de structure autre qu'un élargissement symétrique. L'approximation faite en considérant des molécules d'eau isolées, est donc justifiée par l'interprétation des résultats.

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The Crystal and Molecular Structure of 1,3,7,9-Tetramethyluric Acid.

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Two polymorphic forms of 1,3,7,9-tetramethyluric acid have been found. The form crystallizing as needles is monoclinic, space group $P2_1/a$ with four molecules in a unit cell of dimensions

$$a = 10.11, b = 14.89, c = 6.75 \text{ \AA}; \beta = 100.4^\circ.$$

Atomic parameters determined from the $hk0$ and $0kl$ sharpened Patterson functions and from structure-factor graphs were refined, together with anisotropic temperature factors, by a three-dimensional least-squares process. The standard deviation in bond length is 0.011 \AA . Bond lengths in the five-membered ring are significantly different from those in a purine where this ring does not contain methyl groups or an oxygen atom as substituents. Molecules are stacked almost perpendicular to the c axis, in parallel planes of alternate spacing $3.39, 3.36 \text{ \AA}$, and these blocks of molecules are related by screw axes. Short intermolecular methyl-oxygen distances indicate that C-H...O hydrogen bonds probably arising from activation of the C-H group are present in the crystal structure.

Introduction

The determination of the crystal structure of 1,3,7,9-tetramethyluric acid forms part of a programme of work on the structures of pyrimidines, purines and related compounds. Theophylline and caffeine, di- and trimethyl substituted hydroxy purines respectively have been the subjects of previous work (Sutor, 1958*a, b*). The structure of a tetramethyl purine derivative in which the base is fully substituted (see Fig. 1) is now given. Unlike the other two, it contains no water of crystallization, and crystallographically it is not isomorphous with them. A preliminary account of this work has been published (Sutor, 1960).

Experimental

Tetramethyluric acid ($C_9H_{12}N_4O_3$) used in this investigation was kindly supplied by Prof. E. Boyland

of the Chester Beatty Research Institute. Crystals were obtained by allowing a hot aqueous solution of the substance to cool slowly. Two polymorphic forms separated from different recrystallizations, but conditions favouring the formation of one in preference to the other are not known.

The form which is obtained more readily is that described by Groth when his c axis is halved, and a preliminary account of its crystal structure has been published by de Santis, Giglio & Liquori (1960), who give the cell dimensions as:

$$a = 15.59, b = 8.87, c = 8.46 \text{ \AA}; \\ \beta = 118^\circ, V = 1033 \text{ \AA}^3.$$

Like crystals of theophylline, these can be referred to the space group $P2_1/a$ if weak 'forbidden' reflexions of the type $h0l$ with h odd are ignored. My

work has shown that the number of 'forbidden' ones is about 17%.

Crystals of the other form which is now to be described in detail are needles elongated along the c axis, and twinning is quite frequent. The unit-cell dimensions obtained from rotation and Weissenberg photographs are:

$$a = 10.11, b = 14.89, c = 6.75 \text{ \AA}; \\ \beta = 100.4^\circ, V = 999 \text{ \AA}^3.$$

The density determined from a mixture of carbon tetrachloride and acetone is 1.482 g.cm.^{-3} , and that calculated for a unit cell containing four molecules 1.488 g.cm.^{-3} . The space group is $P2_1/a-C_{2h}^5$, there being no 'forbidden' reflexions observable on any of the photographs. This, together with the smaller volume of the unit cell and short c axis suggested these crystals were more suitable for a full structure determination. Consequently no further work on the other form was undertaken.

For intensity measurements, the $hk0$, $hk1$, $hk2$ and $hk3$ reflexions were recorded with $\text{Cu } K\alpha$ radiation on Weissenberg photographs, taken about the c axis, using the multiple-film technique and the equi-inclination method. The shape of the crystals, and the difficulty in cutting them, prevented reliable data being obtained about other axes. Accordingly only the $0kl$ reflexions were collected for the determination of approximate z co-ordinates. Visual estimations of the intensities of the 973 observed reflexions (excluding the $0kl$'s) were made, and the resulting values converted to structure amplitudes in the usual way. Correction curves for the variation in reflexion spot-shape on the $hk1$, $hk2$ and $hk3$ layer lines were derived from the harmonic mean of equivalent reflexions for which extended and contracted values could be measured (Phillips, 1954). Six of the $hk3$ low-angle reflexions which were well outside the experimentally determined curve were later corrected by scaling to the calculated structure factors.

Determination and refinement of the atomic co-ordinates

As the c axis is fairly short, the molecules are likely to lie in planes almost perpendicular to it. Except for a keto- and two methyl groups of the five-membered ring, tetramethyluric acid consists of a hexa-substituted six-membered ring assumed to be planar. The sharpened $hk0$ Patterson function shows, around the origin, characteristic and easily recognizable peaks corresponding to the equal and parallel vectors within this symmetrical group. The function also contains a large peak which represents equivalent vectors between two of the symmetrical groups related by a centre of symmetry of the space group and which is located at a distance from the origin equal to the vector distance between the molecular centres of these

groups. There was no ambiguity in fixing the orientation of the group, as one side of the ring is parallel to the a axis. Because of the special orientation of the rings in this projection, there are peaks corresponding to intermolecular vectors between groups related by the glide plane. Two possible positions which also satisfied packing conditions were indicated for the ring. Structure factor graphs for the reflexions 200, 400, 020, 040, 110, 120 and 210 were used to select one position which also corresponded to a better vector distribution, and to locate the remaining four atoms. Nevertheless, the same orientation of the whole molecule in the other position—the only other arrangement giving reasonable agreement between observed and calculated structure factors—was not discarded until refinement proved impossible. The z co-ordinates of the atoms were determined from the $0kl$ sharpened Patterson function and from a consideration of the possible molecular packing. For the usual separation between molecular planes, these co-ordinates must be close to a quarter.

Two-dimensional refinement

The atomic co-ordinates were refined by two dimensional Fourier and difference syntheses (Cochran, 1951), and finally by the method of least-squares. All calculations were carried out on the Ferranti Mercury computer. In the least-squares refinement, use was made of Dr Rollett's structure factors-least-squares programme with scattering factors of Berghuis *et al.* (1955) for carbon, nitrogen and oxygen atoms, and that of McWeeny (1951) for the hydrogen atoms. The programme evaluates the block-diagonal approximation— 3×3 and 6×6 matrices for the co-ordinates and temperature factors of each atom and a 2×2 matrix for the scale factor and overall B -value. Two reflexions 110 and 200 which suffer from extinction, and all non-observed ones were given zero weight; all other reflexions were assigned equal weights. When the R -factor for the $hk0$ terms had reached 16%, the difference synthesis indicated the positions of all twelve hydrogen atoms which were included in subsequent calculations. However, it proved impossible to determine their z co-ordinates with any certainty. In both projections, the overall isotropic temperature factor was 3.3 \AA^2 . The R -factors at the end of the two-dimensional refinement were 11.2% for the (001) projection and 19.0% for the (100). These values exclude reflexions too small to be observed, and 110 and 200. The (001) projection calculated from the final co-ordinates from the three dimensional refinement is shown in Fig. 1.

Three-dimensional refinement

It was desirable to continue the least-squares refinement in three dimensions because of the poor $0kl$ data, and because a short intermolecular distance of 2.96 \AA between a methyl group and oxygen atom needed

considered. These shifts, which would undoubtedly give better agreement between observed and calculated structure factors, would lead to pronounced anisotropy of some of the atoms, thought to be meaningless. At the end of the seventh cycle when changes in atomic co-ordinates were less than the standard deviations, refinement was terminated. The *R*-factor for the observed reflexions is 11.2%. Observed and calculated structure factors are listed in Table 1, and atomic co-ordinates in Table 2. The standard deviations in the co-ordinates calculated using the weighted residuals from the least-squares refinement are

$$\begin{aligned}\sigma(x) &= 0.007, 0.005, 0.004 \text{ \AA} \\ \sigma(y) &= 0.007, 0.005, 0.004 \\ \sigma(z) &= 0.009, 0.007, 0.006\end{aligned}$$

for carbon, nitrogen and oxygen atoms respectively.

Bond lengths and bond angles are given in Tables 3 and 4. The estimated standard deviations are 0.011 Å in C-C, 0.010 Å in C-N and 0.009 Å in C-O bonds.

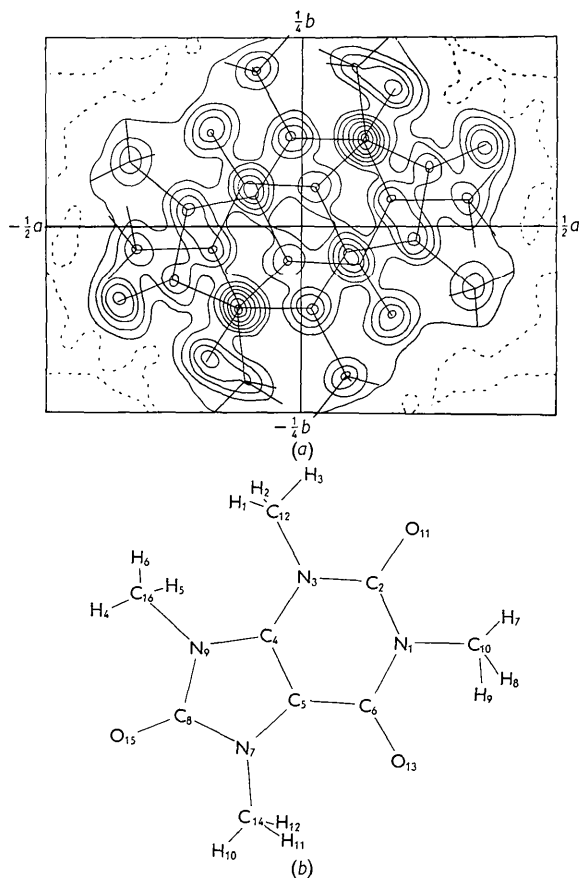


Fig. 1. (a) *hk0* Fourier projection calculated using the final structure factors from the three dimensional refinement. Contours are at intervals of 2 e.Å⁻² with the zero contour broken. The origin is at the centre. (b) 1,3,7,9-Tetramethyluric acid showing the positions of all the atoms and the numbering system used.

Table 3. Comparison of bond lengths and bond angles in theophylline, caffeine and tetramethyluric acid

(a) Bond lengths

Bond	Theophylline	Caffeine	Tetramethyluric acid
C ₄ -C ₅	1.37 Å	1.32 Å	1.349 Å
C ₅ -C ₆	1.41	1.44	1.412
C ₂ -N ₁	1.40	1.42	1.369
C ₂ -N ₃	1.35	1.35	1.387
C ₄ -N ₃	1.37	1.42	1.356
C ₆ -N ₁	1.38	1.36	1.405
C ₄ -N ₉	1.33	1.31	1.369
C ₈ -N ₉	1.31	1.34	1.407
C ₈ -N ₇	1.31	1.32	1.353
C ₅ -N ₇	1.34	1.41	1.386
C ₁₀ -N ₁	1.48	1.48	1.467
C ₁₂ -N ₃	1.46	1.50	1.474
C ₁₄ -N ₇	—	1.47	1.456
C ₁₆ -N ₉	—	—	1.480
C ₂ -O ₁₁	1.19	1.19	1.209
C ₆ -O ₁₃	1.22	1.26	1.237
C ₈ -O ₁₅	—	—	1.227

(b) Bond angles

An atom followed by (H) should be replaced by hydrogen where indicated

Angle	Theophylline	Caffeine	Tetramethyluric acid
C ₂ -N ₁ -C ₆	126.0°	127.6°	126.3°
C ₂ -N ₁ -C ₁₀	115.7	112.0	115.7
C ₆ -N ₁ -C ₁₀	117.7	120.3	118.1
N ₁ -C ₂ -N ₃	117.8	112.9	117.3
N ₁ -C ₂ -O ₁₁	120.8	122.7	121.4
N ₃ -C ₂ -O ₁₁	121.8	124.1	121.3
C ₂ -N ₃ -C ₄	119.4	122.8	118.5
C ₂ -N ₃ -C ₁₂	119.6	117.9	117.3
C ₄ -N ₃ -C ₁₂	121.1	119.2	124.2
N ₃ -C ₄ -C ₅	121.8	121.4	124.0
N ₃ -C ₄ -N ₉	125.5	127.2	128.3
C ₅ -C ₄ -N ₉	112.7	110.9	107.7
C ₄ -C ₅ -C ₆	122.6	119.9	121.1
C ₄ -C ₅ -N ₇	104.2	107.2	108.9
C ₆ -C ₅ -N ₇	133.1	132.8	130.0
N ₁ -C ₆ -C ₅	112.5	115.8	112.9
N ₁ -C ₆ -O ₁₃	121.2	118.4	121.3
C ₅ -C ₆ -O ₁₃	126.5	126.4	125.8
C ₅ -N ₇ -C ₈	106.7	103.4	108.4
C ₅ -N ₇ -C ₁₄ (H)	135.0 (H)	128.7	128.6
C ₈ -N ₇ -C ₁₄ (H)	118.0 (H)	127.5	123.0
N ₇ -C ₈ -N ₉	114.3	112.3	106.7
N ₇ -C ₈ -O ₁₅ (H)	121.0 (H)	112.0 (H)	129.0
N ₉ -C ₈ -O ₁₅ (H)	125.0 (H)	135.0 (H)	124.3
C ₄ -N ₉ -C ₈	102.0	105.7	108.3
C ₄ -N ₉ -C ₁₆	—	—	131.0
C ₈ -N ₉ -C ₁₆	—	—	120.7

Table 4. The C-H bond lengths

Bond	Bond length	Bond	Bond length
C ₁₀ -H ₇	0.9 Å	C ₁₄ -H ₁₀	0.9 Å
C ₁₀ -H ₈	1.0	C ₁₄ -H ₁₁	1.0
C ₁₀ -H ₉	1.1	C ₁₄ -H ₁₂	1.0
C ₁₂ -H ₁	1.1	C ₁₆ -H ₄	0.9
C ₁₂ -H ₂	1.1	C ₁₆ -H ₅	0.9
C ₁₂ -H ₃	1.0	C ₁₆ -H ₆	0.9

Angles have a standard deviation of about 0.7° calculated from the formula of Cruickshank & Robertson (1953).

The least-squares, normal equation of the plane containing the carbon, nitrogen and oxygen atoms is

$$-0.1765x + 0.0406y + 0.9835z - 1.6958 = 0$$

where x , y and z are the co-ordinates (in Å) referred to the orthogonal axes a , b and c' . The average deviation of atoms from this plane is 0.013 Å. The plane of the ring atoms only is given by

$$-0.1797x + 0.0518y + 0.9824z - 1.6990 = 0,$$

and the average deviation of these atoms is 0.004 Å. Table 5 lists the displacements of atoms from these

Table 5. Distance of atoms from (a) the molecular plane, (b) the plane of the purine group whose atoms are starred

Atom	(a) (Å)	(b) (Å)
C ₂	-0.020	-0.009*
C ₄	-0.006	-0.001*
C ₅	0.017	0.007*
C ₆	0.019	0.003*
C ₈	0.002	-0.006*
C ₁₀	-0.018	-0.028
C ₁₂	0.016	0.049
C ₁₄	-0.021	-0.056
C ₁₆	0.014	0.036
N ₁	0.004	-0.001*
N ₃	-0.009	0.006*
N ₇	0.016	-0.002*
N ₉	-0.004	0.003*
O ₁₁	-0.007	0.013
O ₁₃	0.019	-0.011
O ₁₅	-0.024	-0.034

two planes. The deviations from the second plane indicate that the purine group is strictly planar with attached atoms in half the molecule above and in the other half below the plane, except for O₁₁ and O₁₃ whose deviations are not significant. However, as the average deviation of atoms from the molecular plane is only 0.013 Å, maximum 0.024 Å, it is doubtful whether any of these displacements are significant and therefore the molecule can be taken as being planar.

Discussion of the structure

Intramolecular distances

For comparative purposes, Table 3 gives the bond lengths and angles in theophylline, caffeine and tetramethyluric acid. In the comparison of molecular dimensions, the significance tests of Cruickshank & Robertson (1953) were used, and any difference greater than, or equal to 2.5σ has been assumed real. The following discussion shows that the dimensions of the rings are dependent on the presence and nature of substituents.

All three purines have about 1.38 Å for the average of the C-N bonds in the completely substituted

pyrimidine ring. The average length of C-N bonds in the five-membered ring— 1.32 Å for theophylline, 1.35 Å for caffeine and 1.38 Å for tetramethyluric acid—increases as carbon and oxygen atoms are introduced, and finally reaches 1.38 Å on complete substitution. In tetramethyluric acid, all C-N bonds of the five-membered ring are significantly longer than corresponding bonds in theophylline. The shortening of the C₂-N₃ bond observed in adenine hydrochloride (Cochran, 1951), as well as in theophylline and caffeine, has disappeared here.

Exocyclic C-N bonds average 1.469 Å, in good agreement with the single bond value of 1.47 Å. The average of the C=O bonds, 1.224 Å, is not significantly different from their average in theophylline, 1.205 Å, or from the double bond value of 1.20 Å.

There is a striking similarity between the bond angles at N₁ and C₂ for theophylline and tetramethyluric acid, but other angles appear to be affected by the presence of extra methyl and oxygen substituents in the latter. Steric hindrance between O₁₃ and C₁₄ of adjacent rings has caused these two atoms to move away from each other, and a similar but more pronounced effect exists between the two methyl groups C₁₂ and C₁₆. Evidence for this lies in the inequality of pairs of exocyclic angles at C₆, N₇, N₃ and N₉. The same steric effect has been observed in caffeine and probably theophylline where a hydrogen atom is involved. In all three purines, the bond angle C₂-N₃-C₄ is significantly less than C₂-N₁-C₆, possibly a feature of the methyl hydroxy purines.

The dimensions of the pyrimidine ring are similar to Spencer's values (1959) obtained by averaging like bonds in known pyrimidine and purine structures. Discrepancies occur in the N₁-C₆ bond value which in tetramethyluric acid is significantly longer than the predicted value and longer than that found in caffeine and probably theophylline, and in the bond angles particularly C₂-N₃-C₄ which in these methyl hydroxy purines appears to be significantly smaller than the other C-N-C angle. The predicted C=O bond length, 1.22 Å, agrees well with the observed values.

Anisotropic vibration

In Table 6, the maximum, intermediate and minimum values of the axes of the vibration ellipsoids, and their angles referred to the orthogonal axes, a , b and c' are given. No errors can be quoted for suggested shifts in the temperature coefficients are still greater than the standard deviations. The anisotropic vibration of the molecules can be explained in terms of the oscillation of the atoms about the molecular centre. For most atoms, the direction of maximum vibration lies in the molecular plane perpendicular to the bond formed externally to the ring. Most ring atoms have the minimum axis of the vibration ellipsoid perpendicular to the plane, but

Table 6. *Anisotropic temperature factors*

The B values for the axes of the vibration ellipsoids and their angles with respect to the orthogonal axes a , b and c' are given

Atom	B (\AA^2)	Angle with a ($^\circ$)	Angle with b ($^\circ$)	Angle with c' ($^\circ$)
C_2	3.7	63	149	104
	3.2	124	94	146
	2.5	47	59	121
C_4	3.5	67	154	78
	3.0	118	112	143
	2.4	38	77	125
C_5	3.8	81	171	87
	3.1	13	81	81
	1.9	100	89	10
C_6	3.8	60	44	119
	3.3	36	102	58
	3.0	107	49	46
C_8	5.0	69	159	87
	3.8	24	69	81
	2.0	81	90	171
C_{10}	5.5	92	10	100
	3.6	82	99	168
	2.8	9	87	82
C_{12}	4.8	26	69	76
	4.2	99	107	19
	3.1	115	28	78
C_{14}	5.2	38	100	127
	4.3	125	81	144
	3.0	103	167	92
C_{16}	5.2	94	123	33
	4.9	79	36	57
	2.7	12	102	93
N_1	4.1	92	177	88
	2.9	20	91	70
	1.7	110	87	20
N_3	3.2	25	71	74
	3.0	71	161	88
	2.1	106	94	17
N_7	4.0	39	114	119
	3.4	113	74	151
	3.0	119	151	95
N_9	4.0	95	171	98
	3.0	10	96	82
	2.2	99	97	12
O_{11}	4.7	50	136	107
	3.8	127	104	140
	3.5	62	49	125
O_{13}	4.6	48	52	113
	4.3	80	69	24
	3.5	45	134	83
O_{15}	5.2	74	164	86
	4.2	79	91	169
	3.6	19	74	80

exocyclic atoms, which have a greater freedom of movement, have the intermediate value in this direction. This out-of-plane vibration is more pronounced in the case of C_{14} and C_{16} . Under the circumstances, no quantitative analysis of the thermal parameters is possible, but as expected, exocyclic atoms have larger B values than atoms in the ring, an effect which is particularly noticeable for the methyl groups.

Intermolecular distances

Molecules are stacked in parallel planes almost perpendicular to the c axis and of alternate spacing 3.39 and 3.36 \AA . The closest approach distances between layers are $C_4 \cdots C'_6 = 3.44$, 3.35 \AA , $C_2 \cdots N'_7 = 3.39$, 3.36 \AA with atoms below and above respectively. These blocks of molecules are related by screw axes. In the other form of tetramethyluric acid, this close packing is not maintained. Instead there are pairs of molecules in parallel planes 3.5 \AA apart with adjacent pairs practically at right angles to each other.

Table 7. *Intermolecular distances between exocyclic atoms less than 4.5 \AA apart*

Atom in reference molecule at x, y, z	Atom in neighbouring molecule	Intermolecular distance
C_{10}	$C_{10}(1-x, -y, 1-z)$	3.93 \AA
	$C_{12}(\frac{1}{2}+x, \frac{1}{2}-y, z)$	4.17
	$C_{16}(-x, -y, -z)$	3.74
	$C_{16}(-x, -y, 1-z)$	3.84
C_{12}	$C_{16}(1+x, y, z)$	3.87
	$C_{14}(-x, -y, 1-z)$	3.87
	$C_{14}(-x, -y, -z)$	3.92
	$C_{14}(-\frac{1}{2}-x, \frac{1}{2}+y, -z)$	4.13
C_{14}	$C_{16}(\frac{1}{2}+x, \frac{1}{2}-y, z)$	4.10
	$C_{16}(-\frac{1}{2}-x, -\frac{1}{2}+y, -z)$	4.03
C_{16}	$C_{16}(-1-x, -y, -z)$	4.36
	C_{10}	$O_{15}(1+x, y, z)$
$O_{15}(-x, -y, 1-z)$		3.55
$O_{15}(-x, -y, -z)$		3.60
C_{12}		$O_{11}(-\frac{1}{2}+x, \frac{1}{2}-y, z)$
	$O_{13}(-x, -y, 1-z)$	3.68
	$O_{13}(-x, -y, -z)$	3.69
	C_{14}	$O_{15}(-\frac{1}{2}-x, \frac{1}{2}+y, -z)$
$O_{11}(-x, -y, 1-z)$		3.48
$O_{11}(-x, -y, -z)$		3.49
C_{16}		$O_{13}(-\frac{1}{2}+x, -\frac{1}{2}-y, z)$
	$O_{15}(\frac{1}{2}+x, -\frac{1}{2}-y, z)$	3.81
	$O_{11}(-\frac{1}{2}+x, \frac{1}{2}-y, z)$	3.59
	C_{16}	$O_{13}(-x, -y, 1-z)$
$O_{13}(-x, -y, -z)$		3.85
$O_{15}(-1-x, -y, -z)$		3.42
O_{11}		$O_{13}(\frac{1}{2}-x, \frac{1}{2}+y, 1-z)$
	$O_{15}(-x, -y, 1-z)$	4.01
	$O_{15}(-x, -y, -z)$	3.92
	O_{13}	$O_{15}(\frac{1}{2}+x, -\frac{1}{2}-y, z)$

All intermolecular distances between exocyclic atoms less than 4.5 \AA apart are given in Table 7 and some of the shorter intermolecular contacts are shown in Fig. 2. The average $\text{CH}_3 \cdots \text{CH}_3$ separation, 4.00 \AA , agrees with Pauling's value of 4.00 \AA for the sum of the van der Waals radii, but $\text{O} \cdots \text{O}$ distances appear to be long. Two of the $\text{CH}_3 \cdots \text{O}$ lengths (3.00, 3.38 \AA) are less than 3.4 \AA , the sum of the van der Waals radii of methyl and oxygen, the first being much shorter than similar contacts of 3.24 \AA and $\text{CH} \cdots \text{O}$ distances of 3.22 and 3.18 \AA in theophylline and caffeine. Such a close contact might lead to speculation as to the correctness of the proposed atomic arrangement, but there are no other disturbing features such as outstanding disagreement between certain observed and calculated structure factors,

